

Step-By-Step RA Premium Calculator Worked Example

March 21, 2002

This worked example takes the reader through an RA premium calculation for an example farm using the 2003 RA premium calculator. Please refer to the accompanying document "Programming Instructions for Revenue Assurance Premium Calculations for 2003" for the equations referred to in this document by number and the definitions of variables.

The example is for a farm with three basic units of corn and three basic units of soybeans. Corn is grown in three different sections of land. Soybeans are grown in three different sections of land. Basic unit, enterprise unit, and whole-farm premiums are calculated for this farm.

Prices:

The projected harvest price for corn is \$2.30.

The projected harvest price for soybeans is \$4.50.

The example farms reside in Jasper County, Iowa. For Jasper County the reference yield for corn is 121 and the reference yield for soybeans is 39 for soybeans. The prevented planting factors are 1.020 and 1.05 for 65% and 70% prevented planting coverage respectively.

Here are the farm-specific data.

Unit No.	Corn Units				Soybean Units			
	APH yield	BPR	Acreage	Share	APH yield	BPR	Acreage	Share
1	140	0.03590928	100	1.0	50	0.02364661	100	1.0
2	120	0.04205008	100	0.75	35	0.03588003	100	0.75
3	100	0.05161601	100	0.5	40	0.03006825	100	0.5

The Chicago Board of Trade volatilities are
cvpc 0.18 cvps 0.16

Coverage Levels for Basic Units, Enterprise Units, and Whole-Farm Units

The producer selects 75% coverage for basic unit quotes. The per-acre revenue guarantees for basic units are:

Eq (1)

$$\text{revb}(c,1) = 0.75 * 140 * 2.30 = 241.50$$

$$\text{revb}(c,2) = 0.75 * 120 * 2.30 = 207.00$$

$$\text{revb}(c,3) = 0.75 * 100 * 2.30 = 172.50$$

Eq (1)

$$\text{revb}(s,1) = 0.75 * 50 * 4.50 = 168.75$$

$$\text{revb}(s,2) = 0.75 * 35 * 4.50 = 118.13$$

$$\text{revb}(s,3) = 0.75 * 40 * 4.50 = 135.00$$

The producer selects 75% coverage for enterprise unit quotes. The per-acre revenue guarantees for enterprise units are:

Enterprise Units

$$\text{Eq (2)} \quad \text{reve}(c) = .75 * 2.30 * (1.0 * 100 * 140 + 0.75 * 100 * 120 + 0.50 * 100 * 100) / (1.0 * 100 + 0.75 * 100 + 0.50 * 100) = 214.66667 = 214.67$$

$$\text{Eq (2)} \quad \text{reve}(s) = .75 * 4.50 * (1.0 * 100 * 50 + 0.75 * 100 * 35 + 0.5 * 100 * 40) / (1.0 * 100 + 0.75 * 100 + 0.5 * 100) = 144.375 = 144.38$$

The producer selects 85% coverage for a whole-farm unit quote. The per-acre revenue guarantees for the whole-farm unit is:

Whole-Farm Unit

$$\text{Eq (3)} \quad \text{revwf} = .85 * (2.30 * (1.0 * 100 * 140 + 0.75 * 100 * 120 + 0.50 * 100 * 100) + 4.50 * (1.0 * 100 * 50 + 0.75 * 100 * 35 + 0.5 * 100 * 40)) / (1.0 * 100 + 0.75 * 100 + 0.50 * 100 + 1.0 * 100 + 0.75 * 100 + 0.5 * 100) = 203.46$$

Basic Unit Premiums

The first step is to multiply the APH rates, crateou and srateou, by the basic unit discount which is 0.9.

Eq (4)

Unit No.	APH yield	BPR	APH yield	BPR
1	140	0.03231835	50	0.02128195
2	120	0.03784507	35	0.03229203
3	100	0.04645441	40	0.02706143

This farmer does not select the harvest price option for either corn or soybeans.

The coefficients and the value of the rating factors shown in **equation (9)** are given below for the three corn units.

Variable	Coefficient	Variable Value By Unit No.		
		1	2	3
Constant	-0.06702	1	1	1
Rate(c)	0.71182	0.032318	0.037845	0.046454
Rate(c) ²	-0.05698	0.001044	0.001432	0.002158
Cover(c)	0.00038	0.75	0.75	0.75
Cover(c) ²	0.17031	0.5625	0.5625	0.5625
Fyld(c)/yldREF(c)	0.04712	1.157025	0.991736	0.826446
(fyld(c)/yldREF(c)) ²	0.00591	1.338706	0.983539	0.683013
cvp(c)	-0.22933	0.18	0.18	0.18
cvp(c) ²	0.27952	0.0324	0.0324	0.0324
rate(c) x (fyld(c)/yldREF(c))	0.43886	0.024239	0.028384	0.034841
rate(c) x cover(c)	0.04572	0.037393	0.037532	0.038392
rate(c) x cvp(c)	-0.12068	0.005817	0.006812	0.008362
Cover(c) x (fyld(c)/yldREF(c))	-0.0898	0.867769	0.743802	0.619835
cover(c) x cvp(c)	0.22556	0.135	0.135	0.135
(fyld(c)/yldREF(c)) x cvp(c)	-0.00652	0.208264	0.178512	0.14876

The results of multiplying the coefficients by the variable values and the resulting summation of results is given below. The sum is the premium rate for basic units. This rate is rounded to four digits.

Eq (5)

Multiplication result by unit

1	2	3
-0.06702000	-0.06702000	-0.06702000
0.02300485	0.02693888	0.03306718
-0.00005951	-0.00008161	-0.00012296
0.00028500	0.00028500	0.00028500
0.09579938	0.09579938	0.09579938
0.05451901	0.04673058	0.03894215
0.00791176	0.00581272	0.00403661
-0.04127940	-0.04127940	-0.04127940
0.00905645	0.00905645	0.00905645
0.01063742	0.01245652	0.01529024
0.00170961	0.00171598	0.00175529
-0.00070203	-0.00082209	-0.00100910
-0.07792562	-0.06679339	-0.05566116
0.03045060	0.03045060	0.03045060
-0.00135788	-0.00116390	-0.00096992

The corn basic unit rates are

Unit 1	Unit 2	Unit 3
0.04502962	0.05208571	0.06262034

These are rounded to 4 digits.

Corn Basic Unit Premium Rates:

premr(c,1)	premr(c,2)	premrc(c,3)
0.04500000	0.05210000	0.06260000

The results of doing the same process for soybeans is given below.

Eq (5)

Soybean Basic Unit Premium Rates

premr(s,1)	premr(s,2)	premr(s,3)
0.03950000	0.05460000	0.04770000

The premium rate must be adjusted for prevented planting if the farmer selects 65% or 70% prevented planting coverage. This farmer selects 70% prevented planting coverage for corn and soybeans. Then the adjusted premium rate is multiplied by liability (the selected per-acre revenue guarantee) to obtain the per-acre premium.

Eq (8)

$$\begin{aligned} LP(c,1) &= 0.0450*241.50 *1.05 = 11.410188 = 11.41 \\ LP(c,2) &= 0.0521*207.00 *1.05 = 11.323935 = 11.32 \\ LP(c,3) &= 0.0626*172.50 * 1.05 = 11.3384 = 11.34 \end{aligned}$$

Eq (8)

$$\begin{aligned} LP(s,1) &= 0.0395*168.75 *1.05 = 6.9989 = 7.00 \\ LP(s,2) &= 0.0546*118.13 *1.05 = 6.77239 = 6.77 \\ LP(s,3) &= 0.0477*135.00 * 1.05 = 6.761575 = 6.76 \end{aligned}$$

Eq (9)

$$\begin{aligned} TLP(c,1) &= 11.40*100*1.0 = 1,141. \\ TLP(c,2) &= 11.32*100*0.75 = 849 \\ TLP(c,3) &= 11.34*100*0.5 = 567 \end{aligned}$$

Eq (9)

$$\begin{aligned} TLP(s,1) &= 7.00*100*1.0 = 700 \\ TLP(s,2) &= 6.77*100*0.75 = 507.75 = 508 \\ TLP(s,3) &= 6.76*100*0.5 = 338 \end{aligned}$$

Enterprise Unit Premiums

First we need to calculate the variables avgrate(c), efyld(c), avgrate(s), efyld(s), erate(c), and erate(s).

Eq (11)

$$avgrate(c) = (1.0*100*.03231835 + 0.75*100*.03784507+ 0.50*100*.04645441)/ (1.0*100 + 0.75*100 + 0.50*100) = 0.0373$$

Eq (12)

$$efyld(c) = (1.0*100*140 + 0.75*100*120 + 0.50*100*100)/ (1.0*100 + 0.75*100 + 0.50*100) = 124.4444 = 124.4$$

Eq (11)

$$avgrate(s) = (1.0*100*.02128195 + 0.75*100*.03229203+ 0.50*100*.02706143)/ (1.0*100 + 0.75*100 + 0.50*100) = 0.0262$$

Eq (12)

$$efyld(s) = (1.0*100*50 + 0.75*100*35 + 0.50*100*40)/ (1.0*100 + 0.75*100 + 0.50*100) = 42.77778 = 42.8$$

$$erate = 0.0373*(1 - (3 - 1)*.4/9)= 0.033984 = .0340$$

$$esrate = 0.0262*(1 - (3 - 1)*.5/9) = 0.023289 = .0233$$

Eq (13)

$$epremrc = 0.04772 = .0477$$

Eq (13)

$$epremrs = 0.043013 = .0430$$

The premium rate must be adjusted for prevented planting if the farmer selects 65% or 70% prevented planting coverage. This farmer selects 70% prevented planting coverage for corn and soybeans. Then the

adjusted premium rate is multiplied by liability (the selected per-acre revenue guarantee) to obtain the per-acre premium.

$$\text{Eq (16)} \quad \text{LEP(c)} = 0.0477 * 214.67 * 1.05 = 10.751747 = 10.75$$

$$\text{Eq (16)} \quad \text{LEP(s)} = 0.0430 * 144.38 * 1.05 = 6.518757 = 6.52$$

Total loaded premium is found by multiplying by insured acres on each unit (and by option factors which are set to one so they do not appear here), rounding to zero and summing across units.

$$\text{Eq (17)} \quad \text{TLP(c)} = 1075 + 806 + 538 = 2,419$$

$$\text{Eq (17)} \quad \text{TLEP(s)} = 652 + 489 + 326 = 1,467$$

Whole-Farm Unit Premiums

This farmer does not select the harvest price option for either corn or soybeans.

Below are the values of the variables, the coefficients, and the result of multiplying the two together. The rate for the whole-farm unit equals the sum of the results in the last column. These calculations are presented on pages 10 – 18 of the programming instructions.

Index	Variable Value	Result of Coefficient Multiplication
1	1	-0.02171
2	0.034	-0.10031
3	0.0233	0.90903
4	0	0
5	0	0
6	0	0
7	0	0
8	0.001156	-0.19842
9	0.000543	-0.26458
10	0	0
11	0	0
12	0	0
13	0	0
14	0.000792	0.39732
15	0	0
16	0	0
17	0	0
18	0	0
19	0	0
20	0	0
21	0	0
22	0	0
23	0	0
24	0	0
25	0	0
26	0	0

27	0	0	0
28	0	0	0
29	0.85	-0.08366	-0.07112
30	0.7225	0.18319	0.132355
31	0.0289	0.26057	0.00753
32	0.019805	0.16385	0.003245
33	0	0	0
34	0	0	0
35	0	0	0
36	0	0	0
37	0.5979	0.016636	0.009947
38	0.4021	0	0
39	0	0	0
40	0	0	0
41	0	0	0
42	0	0	0
43	0.357484	-0.30912	-0.11051
44	0.161684	0	0
45	0	0	0
46	0	0	0
47	0	0	0
48	0	0	0
49	0.21374	0.29311	0.062649
50	0.065013	0	0
51	0	0	0
52	0	0	0
53	0	0	0
54	0	0	0
55	0.020329	0.60648	0.012329
56	0.013931	-1.25369	-0.01747
57	0	0	0
58	0	0	0
59	0	0	0
60	0	0	0
61	0.013671	0	0
62	0.009369	0	0
63	0	0	0
64	0	0	0
65	0	0	0
66	0	0	0
67	0	0	0
68	0	0	0
69	0	0	0
70	0	0	0
71	0	0	0
72	0	0	0
73	0	0	0

74	0	0	0
75	0	0	0
76	0	0	0
77	0	0	0
78	0	0	0
79	0	0	0
80	0	0	0
81	0	0	0
82	0	0	0
83	0	0	0
84	0	0	0
85	0	0	0
86	0	0	0
87	0	0	0
88	0	0	0
89	0	0	0
90	0	0	0
91	0.012154	0.48512	0.005896
92	0.008329	0.28393	0.002365
93	0	0	0
94	0	0	0
95	0	0	0
96	0	0	0
97	0.005497	0	0
98	0.003767	0	0
99	0	0	0
100	0	0	0
101	0	0	0
102	0	0	0
103	0	0	0
104	0	0	0
105	0	0	0
106	0	0	0
107	0	0	0
108	0	0	0
109	0	0	0
110	0	0	0
111	0	0	0
112	0	0	0
113	0	0	0
114	0	0	0
115	0	0	0
116	0	0	0
117	0	0	0
118	0	0	0
119	0	0	0
120	0	0	0

121	0	0	0
122	0	0	0
123	0	0	0
124	0	0	0
125	0	0	0
126	0	0	0
127	0.303862	0.34494	0.104814
128	0.137432	0	0
129	0	0	0
130	0	0	0
131	0	0	0
132	0	0	0
133	0.181679	-0.35668	-0.0648
134	0.055261	0	0
135	0	0	0
136	0	0	0
137	0	0	0
138	0	0	0
139	1.028099	-0.00795	-0.00817
140	1.097436	-0.00901	-0.00989
141	0	0	0
142	0	0	0
143	0	0	0
144	0	0	0
145	1.056988	0.001367	0.001445
146	1.204366	0.000801	0.000965
147	0	0	0
148	0	0	0
149	0	0	0
150	0	0	0
151	1.486944	-0.00034	-0.0005
152	0	0	0
153	0	0	0
154	0	0	0
155	0	0	0
156	0	0	0
157	0	0	0
158	0	0	0
159	0	0	0
160	0	0	0
161	0	0	0
162	0	0	0
163	0	0	0
164	0	0	0
165	0	0	0
166	2.211001	0.000004	8.84E-06
167	0	0	0

168	0	0	0
169	0	0	0
170	0	0	0
171	0	0	0
172	0	0	0
173	0	0	0
174	0	0	0
175	0	0	0
176	0	0	0
177	0	0	0
178	0	0	0
179	0	0	0
180	0	0	0
181	0.18	-0.00555	-0.001
182	0.16	0.088538	0.014166
183	0.2	0	0
184	0.1	0	0
185	0.2	0	0
186	0.2	0	0
187	0.0324	0.049061	0.00159
188	0.0256	0.025041	0.000641
189	0.04	0	0
190	0.01	0	0
191	0.04	0	0
192	0.04	0	0
193	0.00612	0.016171	9.9E-05
194	0.004194	-0.19112	-0.0008
195	0	0	0
196	0	0	0
197	0	0	0
198	0	0	0
199	0.00544	-0.74971	-0.00408
200	0.003728	0.016195	6.04E-05
201	0	0	0
202	0	0	0
203	0	0	0
204	0	0	0
205	0.0068	0	0
206	0.00466	0	0
207	0	0	0
208	0	0	0
209	0	0	0
210	0	0	0
211	0.0034	0	0
212	0.00233	0	0
213	0	0	0
214	0	0	0

215	0	0	0
216	0	0	0
217	0.0068	0	0
218	0.00466	0	0
219	0	0	0
220	0	0	0
221	0	0	0
222	0	0	0
223	0.0068	0	0
224	0.00466	0	0
225	0	0	0
226	0	0	0
227	0	0	0
228	0	0	0
229	0.001102	-0.21696	-0.00024
230	0.000755	0.40974	0.000309
231	0	0	0
232	0	0	0
233	0	0	0
234	0	0	0
235	0.00087	1.58392	0.001379
236	0.000596	-0.30456	-0.00018
237	0	0	0
238	0	0	0
239	0	0	0
240	0	0	0
241	0.00136	0	0
242	0.000932	0	0
243	0	0	0
244	0	0	0
245	0	0	0
246	0	0	0
247	0.00034	0	0
248	0.000233	0	0
249	0	0	0
250	0	0	0
251	0	0	0
252	0	0	0
253	0.00136	0	0
254	0.000932	0	0
255	0	0	0
256	0	0	0
257	0	0	0
258	0	0	0
259	0.00136	0	0
260	0.000932	0	0
261	0	0	0

262	0	0	0
263	0	0	0
264	0	0	0
265	0.107622	0.010022	0.001079
266	0.095664	-0.1312	-0.01255
267	0.11958	0	0
268	0.05979	0	0
269	0.11958	0	0
270	0.11958	0	0
271	0.072378	0	0
272	0.064336	0	0
273	0.08042	0	0
274	0.04021	0	0
275	0.08042	0	0
276	0.08042	0	0
277	0	0	0
278	0	0	0
279	0	0	0
280	0	0	0
281	0	0	0
282	0	0	0
283	0	0	0
284	0	0	0
285	0	0	0
286	0	0	0
287	0	0	0
288	0	0	0
289	0	0	0
290	0	0	0
291	0	0	0
292	0	0	0
293	0	0	0
294	0	0	0
295	0.064347	0.042676	0.002746
296	0.057198	0.051441	0.002942
297	0.071497	0	0
298	0.035748	0	0
299	0.071497	0	0
300	0.071497	0	0
301	0.029103	0	0
302	0.02587	0	0
303	0.032337	0	0
304	0.016168	0	0
305	0.032337	0	0
306	0.032337	0	0
307	0	0	0
308	0	0	0

309	0	0	0
310	0	0	0
311	0	0	0
312	0	0	0
313	0	0	0
314	0	0	0
315	0	0	0
316	0	0	0
317	0	0	0
318	0	0	0
319	0	0	0
320	0	0	0
321	0	0	0
322	0	0	0
323	0	0	0
324	0	0	0
325	0	0	0
326	0	0	0
327	0	0	0
328	0	0	0
329	0	0	0
330	0	0	0

The whole-farm premium rate for this example is 0.06326, which is rounded to .0633.

Again, this rate is found by multiplying all the variable values as shown in the second column of Table 1 beginning on page 9 of “Programming Instructions for Revenue Assurance Premium Calculations for 2002” by the appropriate column of whole-farm coefficients found .

Now we need to check to see if 0.0633 is less than 50% of the average enterprise unit premium rate. The enterprise unit premium rates using the whole-farm coverage level are found using equations (18).

Enterprise unit premium rates using whole-farm coverage level.

Corn	Soybeans
0.07130	0.066900

The weighted average of these two equals 0.0691. **Equation (19)**

$$.0691 = ((1.0*100 + 0.75*100 + 0.50*100)*0.0713+(1.0*100 + 0.75*100 + 0.50*100)*0.0669)/(1.0*100 + 0.75*100 + 0.50*100+1.0*100 + 0.75*100 + 0.50*100)$$

50% of this average rate is 0.03455, which is less than the whole-farm rate of 0.0633, so the 50% maximum discount has not been exceeded.

The whole-farm prevented planting coverage is 70%. Thus the per-acre whole-farm premium equals:

$$\text{Eq (23)} \quad \text{LWFP} = 0.0633*203.46*1.05 = 13.52296 = 13.52$$

This equation would be more complicated except that the preventing planting factors for corn and soybeans are identical. If they were different then 1.05 in the above equation would be replaced by the weighted average of the corn and soybean 70% prevented planting factors.

The total loaded whole-farm premium is found by multiplying by insured acres on each unit (and by option factors which are set two one so they do not appear here), rounding to zero, and then summing across all units.

$$\text{Eq (29)} \quad \text{TLWFP} = 1352 + 1014 + 676 + 1352 + 1014 + 676 = 6084$$

Premium Subsidy

To calculate the producer paid premium we need calculate premium subsidy. For basic units the subsidy factor is 0.55 because the coverage level percent is 0.75. The subsidies are rounded to whole-dollar amounts.

Eq (25)

$$psub(c,1) = 0.55 * 1141 = 628$$

$$psub(c,2) = 0.55 * 849 = 467$$

$$psub(c,3) = 0.55 * 567 = 312$$

$$psub(s,1) = 0.55 * 700 = 385$$

$$psub(s,2) = 0.55 * 508 = 279$$

$$psub(s,3) = 0.55 * 338 = 186$$

Eq (26)

$$psube(c,1) = 0.55 * 1075 = 591$$

$$psube(c,2) = 0.55 * 806 = 443$$

$$psube(c,3) = 0.55 * 538 = 296$$

$$psube(c) = 591 + 443 + 296 = 1330$$

$$psube(s,1) = 0.55 * 652 = 359$$

$$psube(s,2) = 0.55 * 489 = 269$$

$$psube(s,3) = 0.55 * 326 = 179$$

$$psube(s) = 359 + 269 + 179 = 807$$

Eq (27)

$$psubwf(c,1) = 0.38 * 1352 = 514$$

$$psubwf(c,2) = 0.38 * 1014 = 385$$

$$psubwf(c,3) = 0.38 * 676 = 257$$

$$psubwf(s,1) = 0.38 * 1352 = 514$$

$$psubwf(s,2) = 0.38 * 1014 = 385$$

$$psubwf(s,3) = 0.38 * 676 = 257$$

$$psubwf = 514 + 385 + 257 + 514 + 385 + 257 = 2312$$

Producer Paid Premium

Producer paid premium for corn and soybean basic units:

Eq (28)

$$TLPsub(c,1) = 1141 - 628 = 513$$

$$TLPsub(c,2) = 849 - 467 = 382$$

$$TLPsub(c,3) = 567 - 312 = 255$$

Eq (28)

$$TLPsub(s,1) = 700 - 385 = 315$$

$$TLPsub(s,2) = 508 - 279 = 229$$

$$TLPsub(s,3) = 338 - 179 = 152$$

Producer paid premium for corn enterprise unit

Eq (29)

$$TLEPsub(c) = 2,419 - 1,330 = 1,089$$

Producer premium for soybean enterprise unit

Eq (29)

$$TLEPsub(s) = 1,467 - 807 = 660$$

Producer premium for whole-farm unit

Eq (30)

$$TLWFP_{\text{sub}} = 6,084 - 2,312 = 3,772$$

Optional Units

This example is for a farm in Jasper County that has optional units. Please refer to the first page of this document for relevant data.

Here are the farm-specific data.

Unit No.	Corn Units				Soybean Units			
	APH yield	BPR rate	Acreage	Share	APH yield	BPR rate	Acreage	Share
1	140	0.03590900	100	1.0	35	0.03588000	100	1.0
2	100	0.05161600	100	1.0	40	0.03006800	100	1.0

The per-acre selected revenue guarantee is given below. The coverage level for both corn and soybeans is 0.750. Prevented planting coverage is 0.70.

Per-acre revenue guarantees:

Unit No.	Corn	Soybeans
1	241.50	118.13
2	172.50	135.00

Base premium rates using equation (5):

Unit No.	Corn	Soybeans
1	0.0450	0.0546
2	0.0626	0.0477

Per-acre premiums using equations (9):

Unit No.	Corn	Soybeans
1	11.41	6.77
2	11.34	6.76

Optional Unit Premiums

Here we use equation (14) to find the optional unit premiums.

$$\begin{aligned} TLP(c,1) &= 11.41 * 100 * 1.0 * 1.1 = 1255.1 = 1,255 & TLP(s,1) &= 6.77 * 100 * 1.0 * 1.10 = 744.7 = 745 \\ TLP(c,2) &= 11.34 * 100 * 1.0 * 1.1 = 1247.4 = 1,247 & TLP(s,2) &= 6.76 * 100 * 1.0 * 1.10 = 743.6 = 744 \end{aligned}$$

Subsidies by Unit

Eq (31)

$$\begin{aligned} psub(c,1) &= 0.55 * 1255 = 690.25 = 690 \\ psub(c,2) &= 0.55 * 1247 = 685.85 = 686 \end{aligned}$$

$$\begin{aligned} psub(s,1) &= 0.55 * 745 = 409.75 = 410 \\ psub(s,2) &= 0.55 * 744 = 409.20 = 409 \end{aligned}$$

Producer Paid Premiums

Eq (51)

$$\begin{aligned} TLP_{\text{sub}}(c,1) &= 1255 - 690 = 565 \\ TLP_{\text{sub}}(c,2) &= 1247 - 686 = 561 \end{aligned}$$

Eq (52)

$$\begin{aligned} TLP_{\text{sub}}(s,1) &= 745 - 410 = 335 \\ TLP_{\text{sub}}(s,2) &= 744 - 409 = 335 \end{aligned}$$